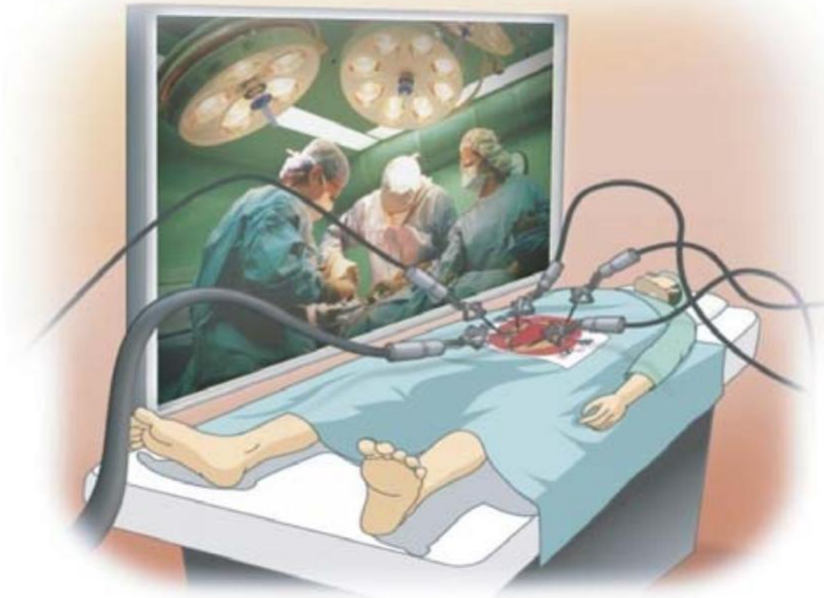


# Theoretical Study of Scalable Three-dimensional Radiated Sound Field Reproduction System with Directional Loudspeakers and Wave Field Synthesis

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# Introduction

- Ultra-realistic communication (URC)
  - Create a "realistic sensation"
  - Use 3D video and 3D audio
- Use Cases
  - Remote operation
  - Teleconference



# Introduction

- Future 3D Television
  - 3D image emitting sound pops up in 3D space
  - People enjoy the sound of the 3D image from any direction without wearing any equipment



**3D sound technology  
that allows people to  
hear 3D sound images  
without wearing  
headphones**

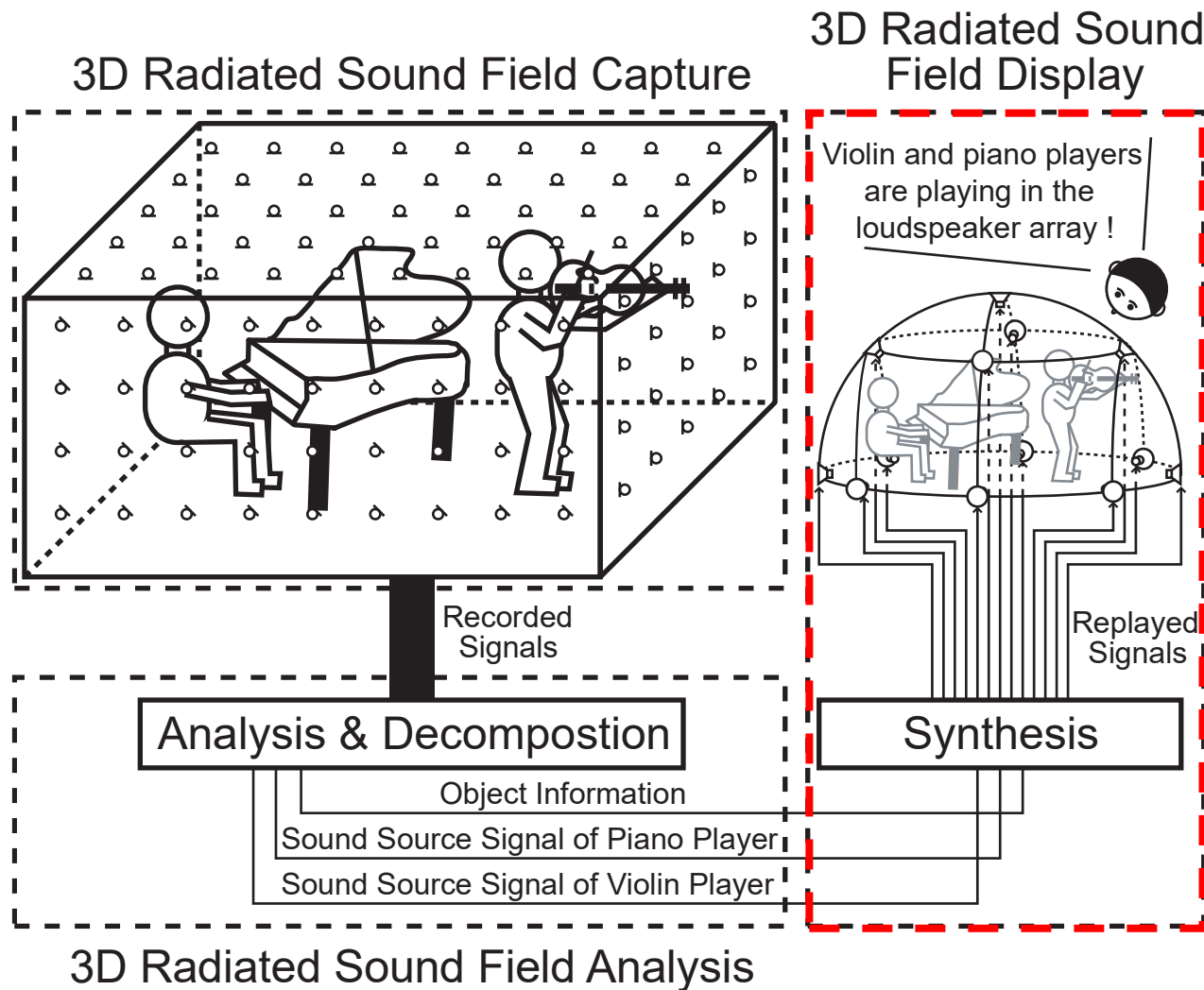
# My previous study

- 3D audio for future 3D TV

- Component

- Capture
- Analysis
- Display

T. Kimura, Y. Yamakata, M. Katsumoto, T. Okamoto, S. Yairi, Y. Iwaya and Y. Suzuki: "Three-dimensional radiated sound field display system using directional loudspeakers and wave field synthesis", Acoust. Sci. & Tech., 33, 1, pp. 11-20 (2012).

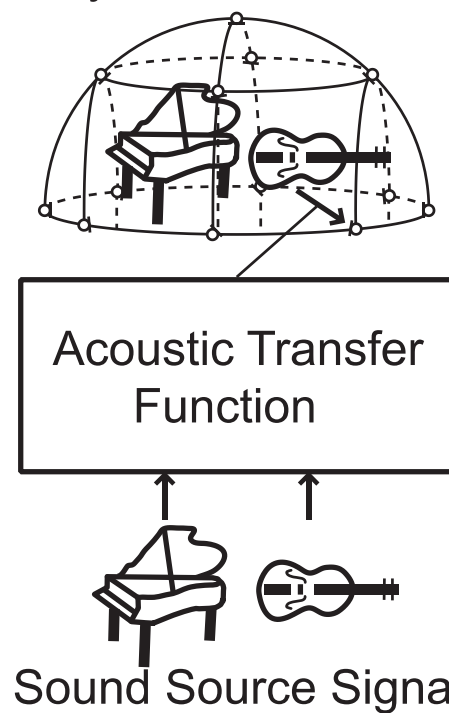


# My previous study

- 3D radiated sound field reproduction system using wave field synthesis

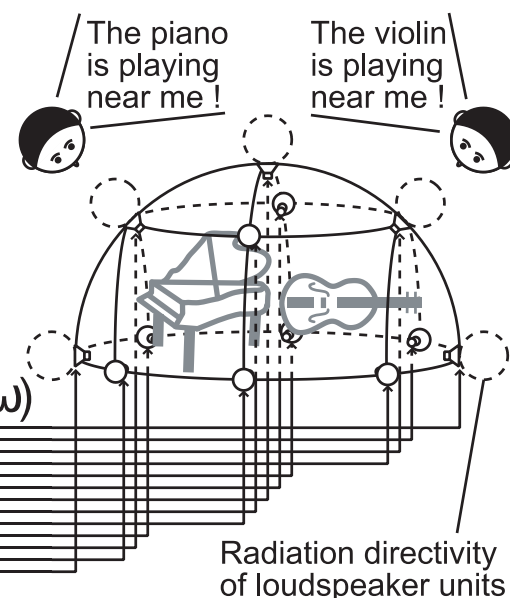
- Problem

- The size of the microphone array is the same as the loudspeaker array
  - It takes a great deal of effort to create an acoustic transfer function database
2. Multichannel audio signals  $P(\mathbf{r}_i, \omega)$  are synthesized



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1. Radiated loudspeaker array is placed



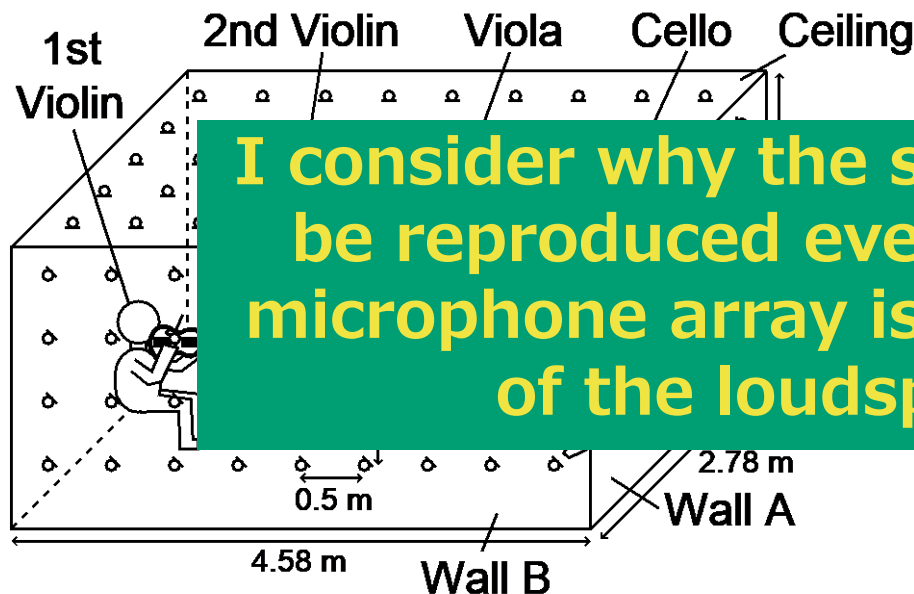
3. Synthesized multichannel audio signals are played from radiated loudspeaker array





# My previous study

- Demonstration of radiated loudspeaker array
  - YouTube
    - <https://www.youtube.com/watch?v=hntR0yt-HDw>
  - Despite the difference in size between the microphone array and the loudspeaker array, it felt as if a string quartet was being played inside the loudspeaker array



**I consider why the sound field seems to be reproduced even if the size of the microphone array is different from that of the loudspeaker array**



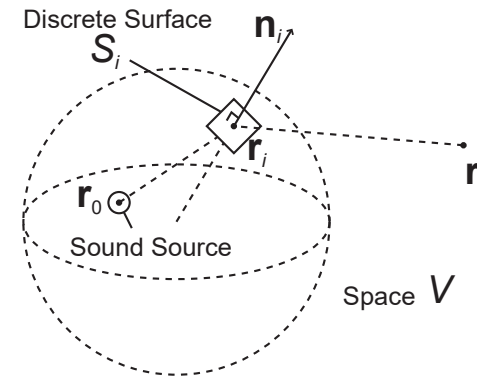
# Theoretical consideration

- Wave field synthesis formula

$$P(\mathbf{r}, \omega) = \frac{jk}{4\pi} \sum_{i=1}^M P(\mathbf{r}_i, \omega) D(\theta_i) \frac{e^{-jk|\mathbf{r}-\mathbf{r}_i|}}{|\mathbf{r}-\mathbf{r}_i|} \Delta S_i$$

$$P(\mathbf{r}_i, \omega) = AD_0(\theta_0, \phi_0) \frac{e^{-jk|\mathbf{r}_i-\mathbf{r}_0|}}{|\mathbf{r}_i-\mathbf{r}_0|} \quad k = \frac{\omega}{c}$$

T. Kimura, Y. Yamakata, M. Katsumoto, T. Okamoto, S. Yairi, Y. Iwaya and Y. Suzuki: "Three-dimensional radiated sound field display system using directional loudspeakers and wave field synthesis", Acoust. Sci. & Tech., 33, 1, pp. 11–20 (2012).



- $D(\theta_i)$  : Radiation directivity of loudspeaker unit
- $A$  : Amplitude of sound sources
- $D_0(\theta_0, \phi_0)$  : Radiation directivity of sound sources
- $c$  : Sound velocity

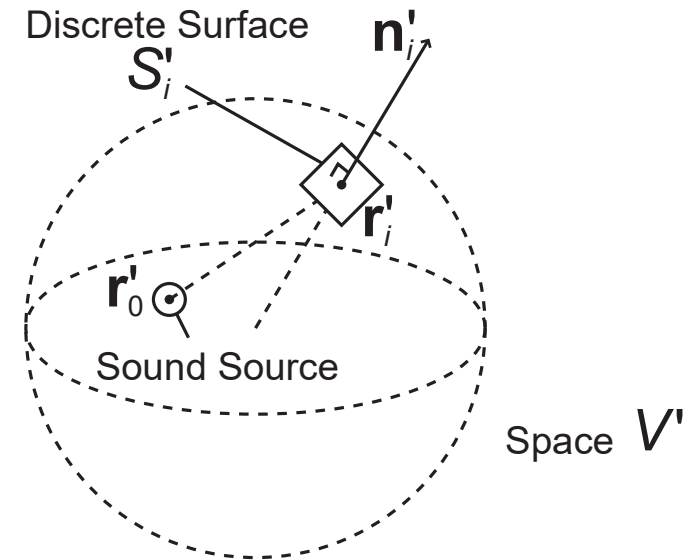


# Theoretical consideration

- Microphone array size :  $\alpha$  times

T. Kimura, "Theoretical Study of Scalable 3D Radiated Sound Field Reproduction System with Directional Loudspeakers and Wave Field Synthesis," Proc. ASJ Spring Meeting, No. 3-Q-8, pp. 225-228 (2024).

$$\begin{aligned} P(\mathbf{r}_i', \omega) &= AD_0(\theta_0, \phi_0) \frac{e^{-jk|\mathbf{r}_i' - \mathbf{r}_0'|}}{|\mathbf{r}_i' - \mathbf{r}_0'|} \\ &= AD_0(\theta_0, \phi_0) \frac{e^{-jk\alpha|\mathbf{r}_i - \mathbf{r}_0|}}{\alpha|\mathbf{r}_i - \mathbf{r}_0|} \\ &= \frac{AD_0(\theta_0, \phi_0)}{\alpha} \frac{e^{-jk'\alpha|\mathbf{r}_i - \mathbf{r}_0|}}{|\mathbf{r}_i - \mathbf{r}_0|} \end{aligned}$$



- $k'$ : Transformed wavenumber

$$k' = \alpha k = \frac{\alpha \omega}{c} = \frac{\omega}{\frac{c}{\alpha}} = \frac{\omega}{c'}$$

$$\mathbf{r}_i' = \alpha \mathbf{r}_i$$

$$\mathbf{r}'_0 = \alpha \mathbf{r}_0$$

$$|\mathbf{r}'_i - \mathbf{r}'_0| = \alpha |\mathbf{r}_i - \mathbf{r}_0|$$

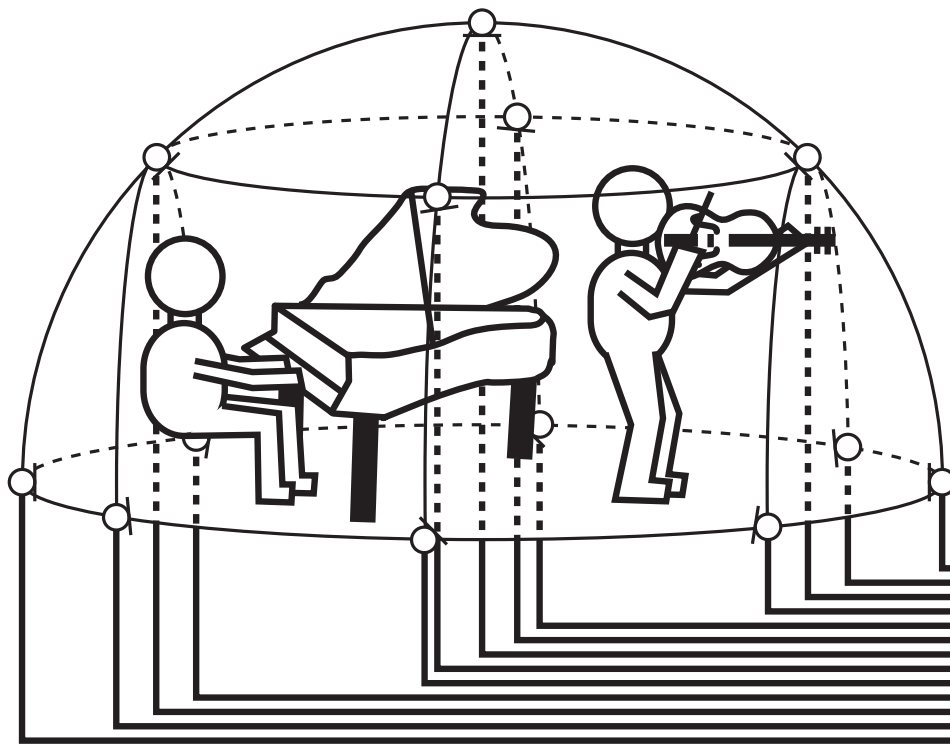
- $c'$  : Transformed speed of sound

**The sound field where the speed of sound has changed to  $1/\alpha$  time**

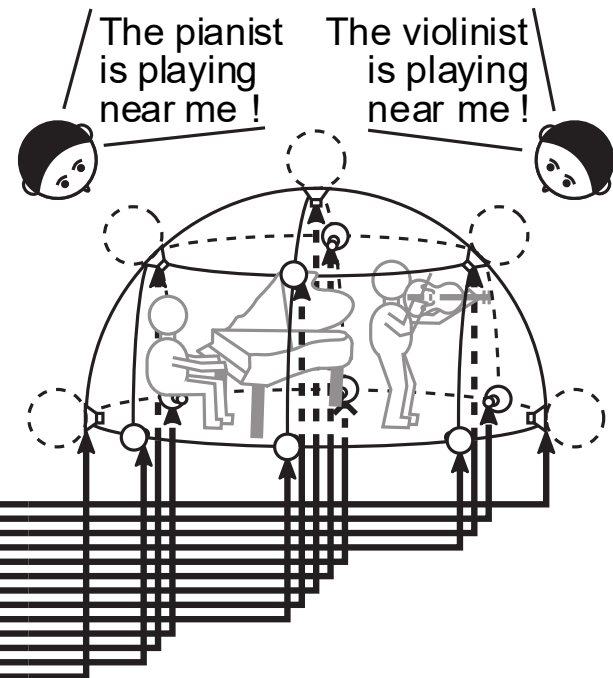
# Theoretical consideration

- Diagram of proposed system
  - Scaled 3D radiated sound field is reproduced
    - The speed of sound changed

Original Sound Field



Reproduced Sound Field



# Conclusion

- 3D radiated sound field reproduction
  - I theoretically investigated the sound field reproduced when the size of the microphone array differs from that of the loudspeaker array



- Scaled 3D radiated sound field is reproduced
  - The condition
    - The arrangement of the microphone and directional loudspeaker is similar
    - The speed of sound changes

# Future works

- Validation by computer simulation
- Acoustic measurements and listening tests by radiated loudspeaker array

